

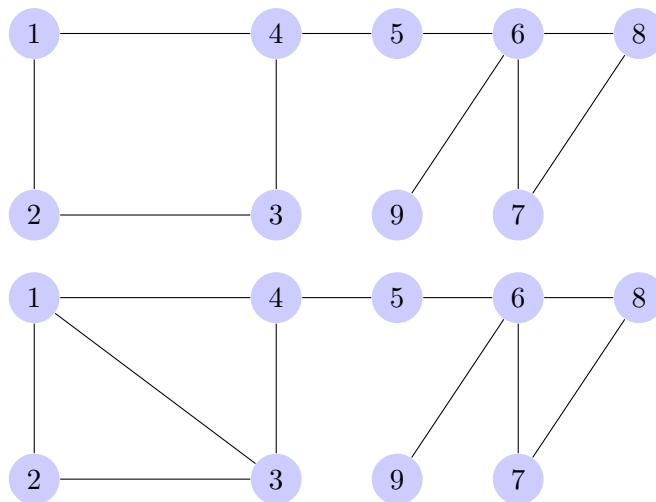
Assignment 10

Issue date: 26 June 2014 **Due date:** 03 July 2014, 11:00
It is explicitly recommended to solve exercises in groups of two.

Exercise 1: Clique number

2+2 Points

Provide the clique numbers ω and the number of ω -cliques for the following two graphs.

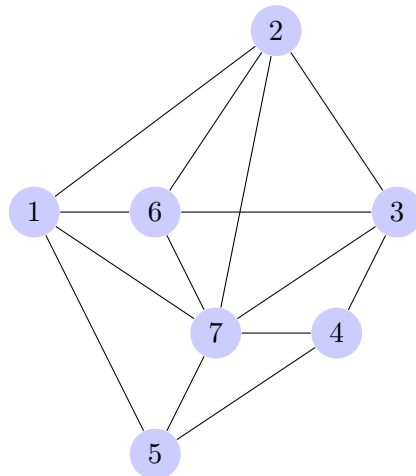


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Exercise 2: Maximal Clique Enumeration

1+2+3 Points

- (a) Modify the following example graph from the lecture by adding edge(s) to it such that the resulting graph has at least two identical maximal cliques at some level i of the binary tree.
- (b) Construct the tree that lists all the maximal cliques of the modified graph.
- (c) Show the lexicographically correct position for the clique(s) that get generated by more than one maximal cliques from the previous level in the tree.



[please turn over]

Exercise 3: n -Cliques**3+3+4 Points**

Consider the adjacency matrix $A = A(G)$ associated with an undirected graph $G = (V, E)$, $V = \{1, \dots, n\}$. It is easily seen that an entry $a_{i,j}^{(2)}$ of the matrix $A^2 = A \cdot A$ is the number of length-2 walks between vertices i and j in G . Use this information to solve the following problems:

- (a) Design a possibly fast algorithm for finding a 3-clique in an undirected graph $G = (V, E)$.
- (b) Design a possibly fast algorithm for finding a 6-clique in an undirected graph $G = (V, E)$.
Hint: Reuse the algorithm designed for the first problem on an appropriate auxiliary graph.
- (c) How can you generalize the algorithms to any fixed k for finding a k -clique in an undirected graph $G = (V, E)$?

Please submit your answers electronically to teaching assistant Habiba (habiba@uni-konstanz.de).